

EE 232: Lightwave Devices

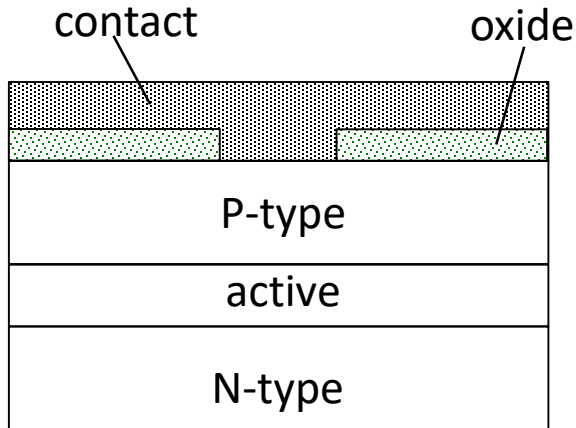
Lecture #17 – Steady state LED and LASER characteristics - Part 2

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4/18/2019

Current and photon confinement

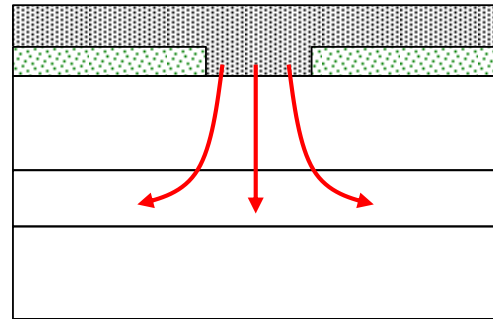


Edge-emitting stripe laser

← lateral direction

↑ transverse direction

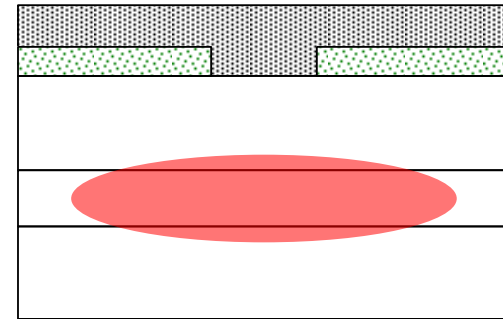
Current confinement



Oxide confines current in lateral direction.

No confinement in lateral direction

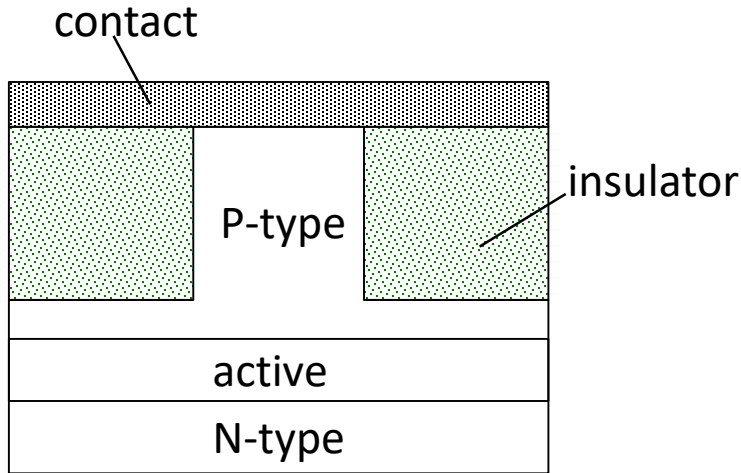
Photon confinement



Index contrast confines mode in transverse direction

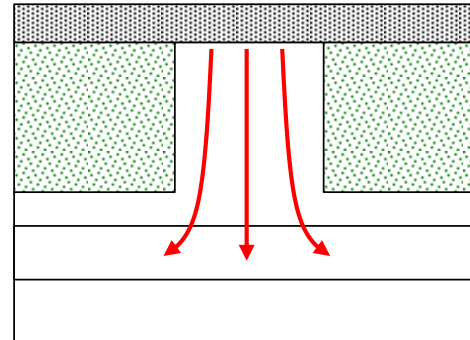
No confinement in lateral direction

Current and photon confinement



Edge-emitting ridge laser

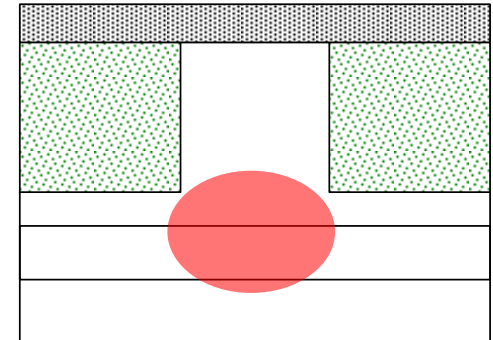
Current confinement



Heterostructure confines current in transverse direction.

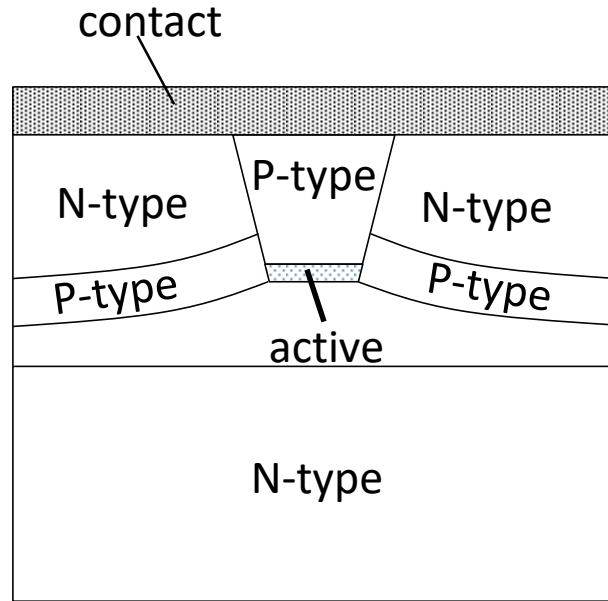
Ridge confines current in lateral direction.

Photon confinement



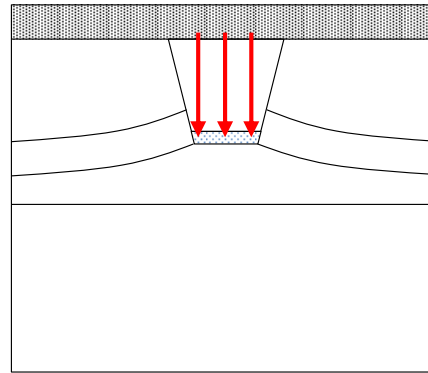
Index contrast confines mode in transverse and lateral direction

Current and photon confinement



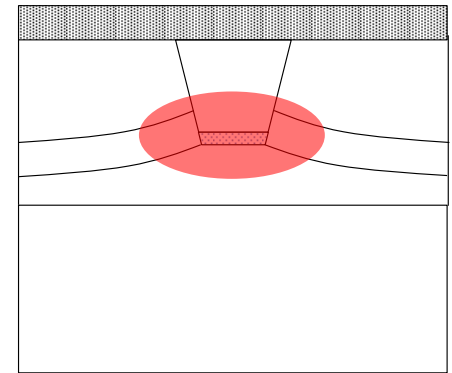
Edge-emitting buried ridge stripe

Current confinement



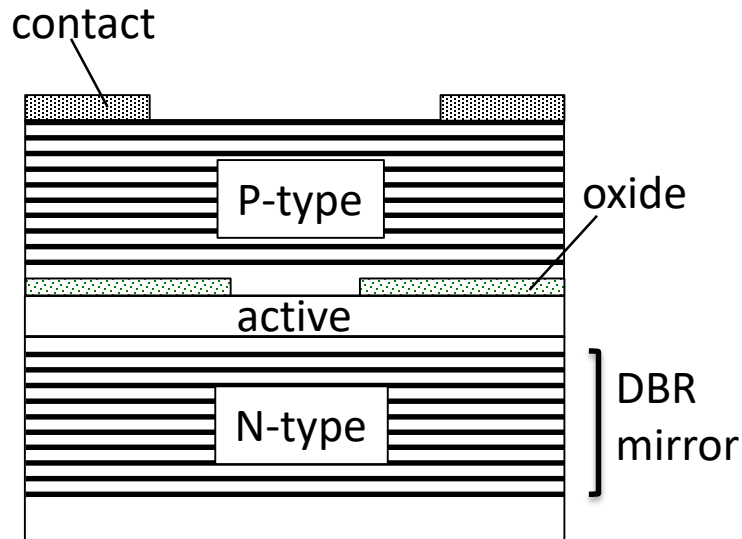
Heterostructure and reverse-biased pn junction confines current in transverse and lateral direction.

Photon confinement



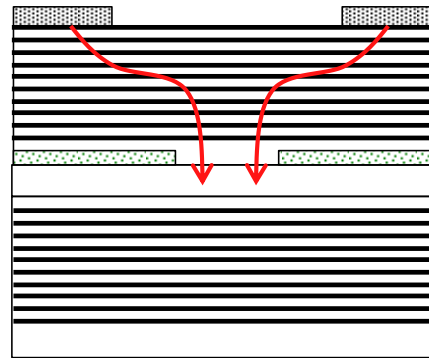
Index contrast confines mode in transverse and lateral direction

Current and photon confinement



Surface-emitting
oxide aperture laser

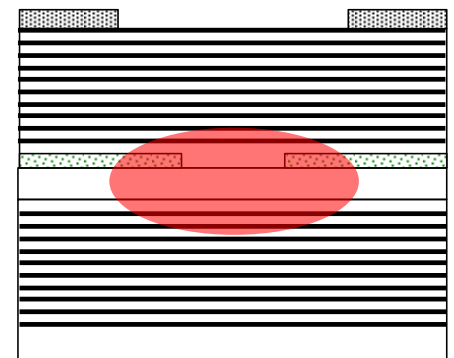
Current confinement



Oxide confines current
in lateral direction.

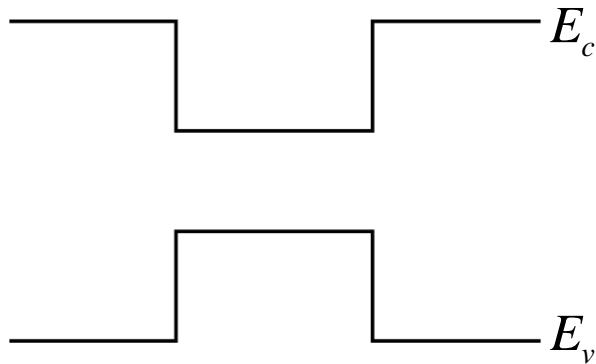
Heterostructure
confines current
in transverse direction

Photon confinement

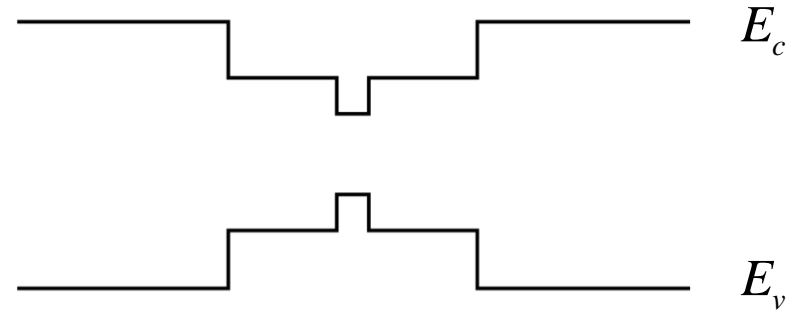


Index contrast confines
mode in transverse and
lateral direction

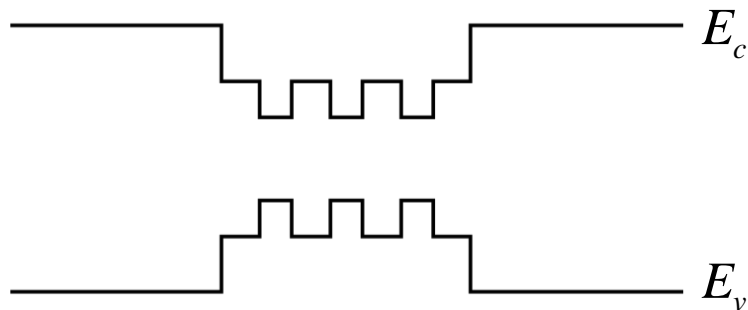
Current and photon confinement



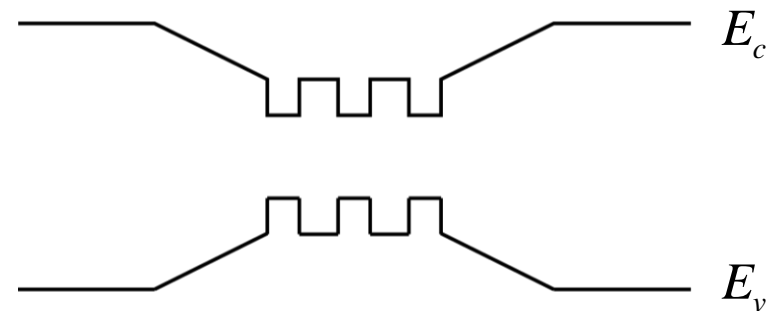
Double heterostructure



Single quantum well separate confinement heterostructure



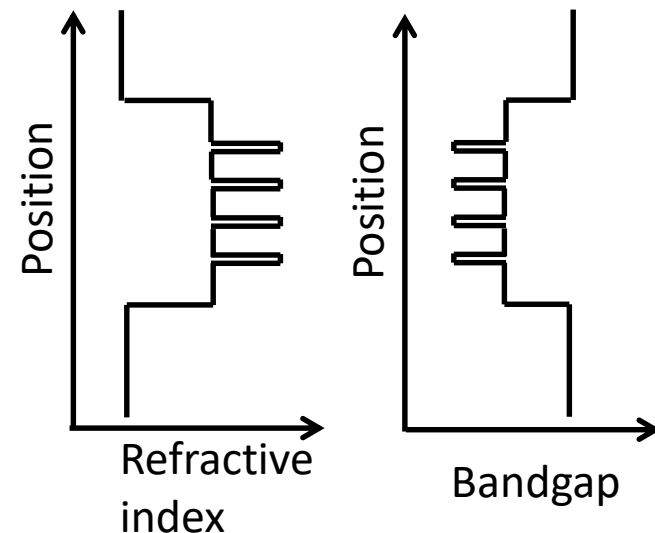
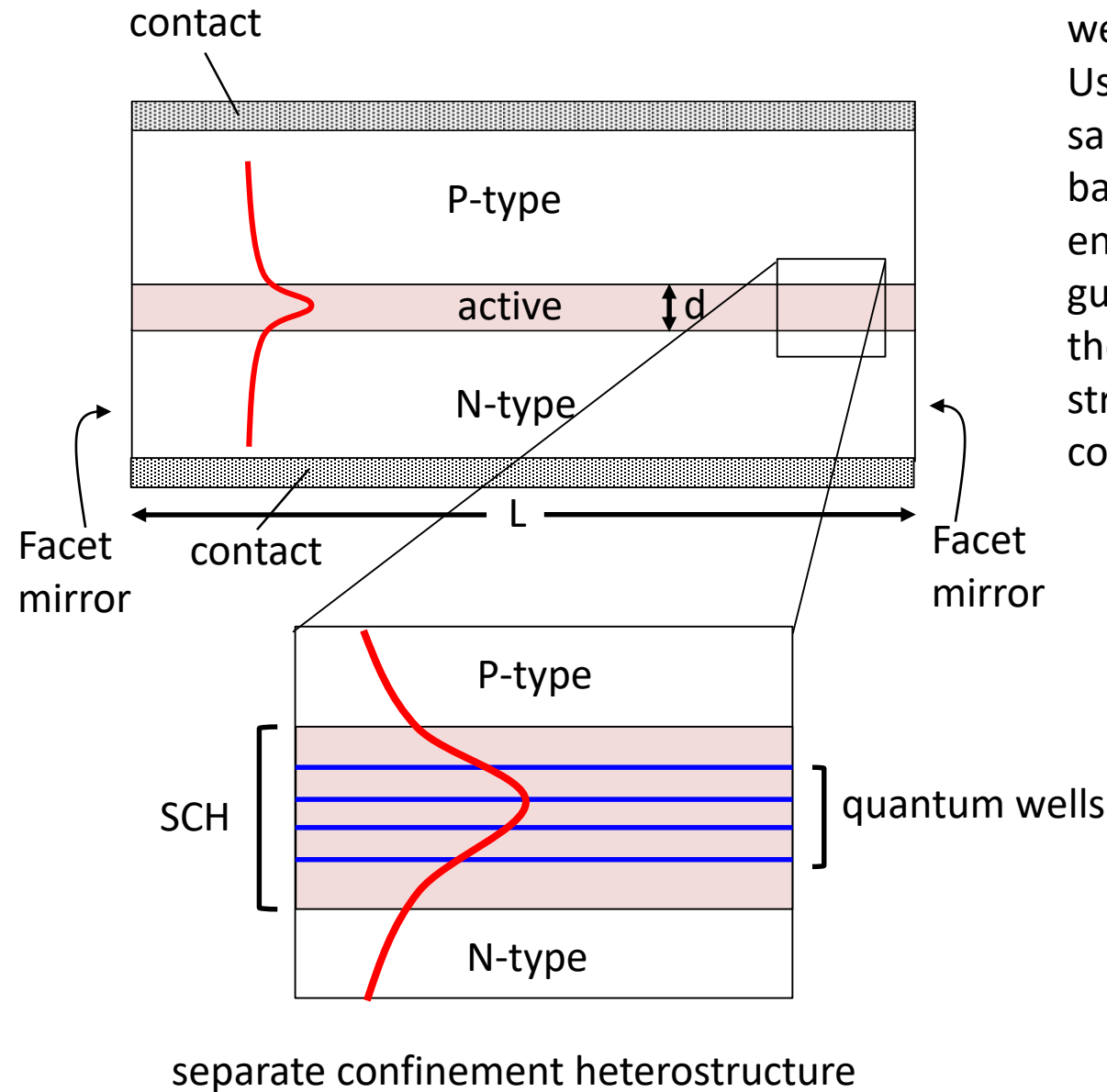
Multiple quantum well (MQW) separate confinement heterostructure



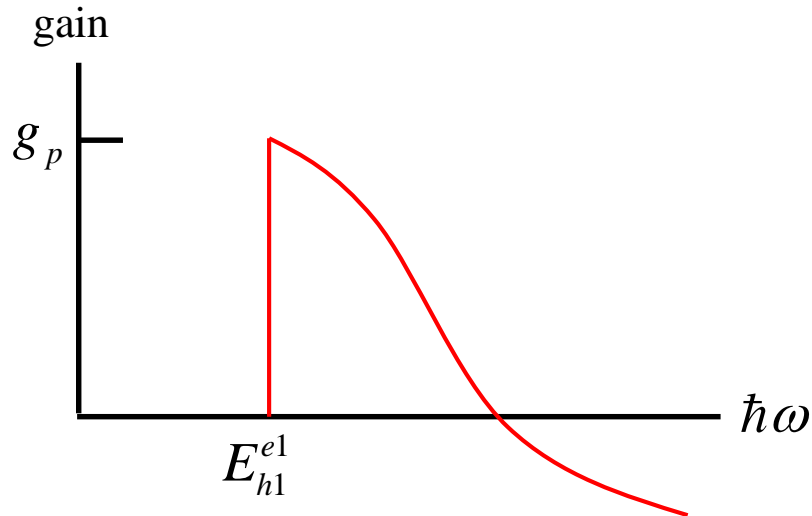
Graded index separate confinement heterostructure (GRIN SCH)

Quantum well laser

Quantum well(s) can only very weakly confine a mode. Usually, quantum wells are sandwiched inside another higher bandgap material that can be engineered to improve mode guiding and electron injection into the quantum well(s). This type of structure is called a separate confinement heterostructure (SCH).



Gain in quantum well



Peak gain occurs at the bandedge

$$g_p = g_m (f_c[\hbar\omega = E_{hl}^{e1}] - f_v[\hbar\omega = E_{hl}^{e1}])$$

Assuming only subband is filled in conduction and valence bands we can write an approximate expression for the peak gain

Recall,

$$n = n_c \ln(1 + \exp[(F_c - E_g - E_{e1})/kT]) \quad n_c = \frac{m_e^* kT}{\pi \hbar^2 L_z} \quad n_v = \frac{m_h^* kT}{\pi \hbar^2 L_z}$$

$$p = n_v \ln(1 + \exp[(E_{hl} - F_v)/kT])$$

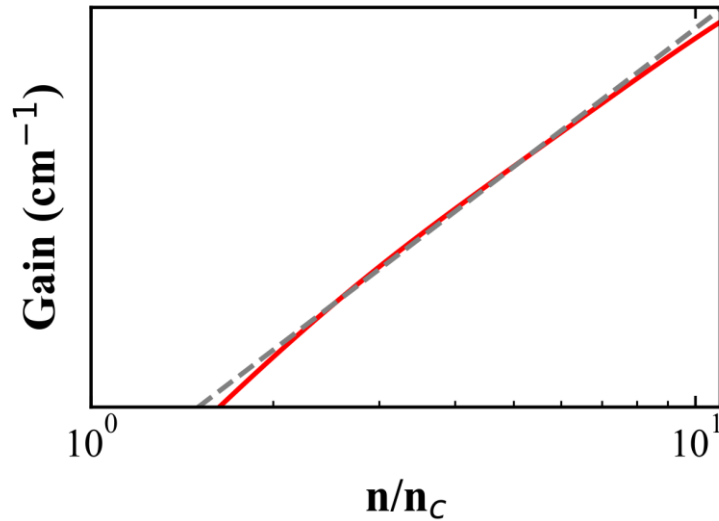
The Fermi functions can be written in terms of the carrier density

$$f_c(\hbar\omega = E_{hl}^{e1}) = \frac{1}{1 + \exp\left[\frac{(E_g + E_{e1} - F_c)}{kT}\right]} = 1 - \exp(-n/n_c)$$

$$f_v(\hbar\omega = E_{hl}^{e1}) = \frac{1}{1 + \exp\left[\frac{(E_{hl} - F_v)}{kT}\right]} = \exp(-p/n_v)$$

Then,
$$g_p = g_m [1 - \exp(-n/n_c) - \exp(-p/n_v)]$$

Gain in quantum well



$$g_p = g_m [1 - \exp(-n/n_c) - \exp(-p/n_v)]$$

The plot of peak gain vs. carrier concentration (red line) is approx. linear on a semi-log plot, therefore a simpler approximate expression is often used (dashed gray curve).

$$g_p = g_0 \ln[n/n_0]$$

As discussed previously, the current density can be written in terms of a polynomial of the carrier density (e.g. $J \propto n^2$ if spontaneous emission dominates). Therefore, we can write a similar approximate expression for peak gain in terms of carrier density.

$$g_p = g_0 \ln[J/J_0]$$

Note: g_0 are not the same in both expressions

Quantum well laser - threshold gain

$$g_w = g_0 \ln\left(\frac{J_w}{J_0}\right)$$

$$n_w \Gamma_w g_w = \alpha_i + \frac{1}{2L} \ln\left(\frac{1}{R_1 R_2}\right)$$

g_w : quantum well threshold gain

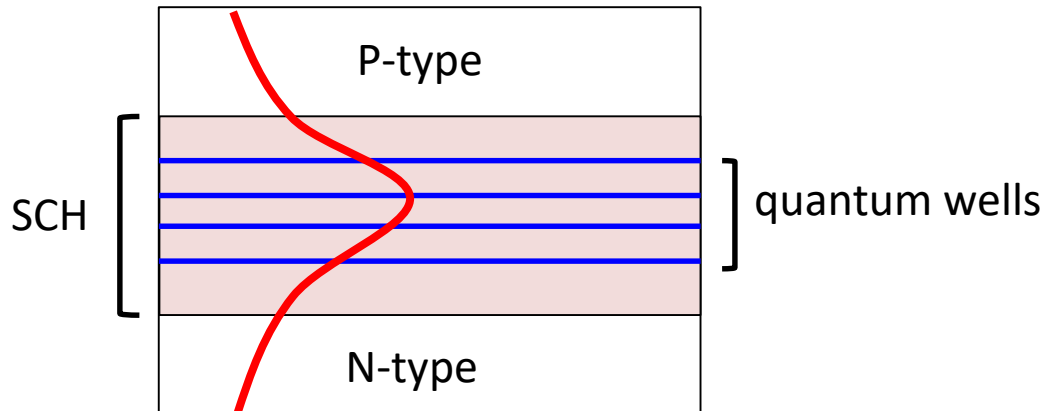
J_w : threshold quantum well current density

n_w : number of quantum wells in active region

Γ_w : fraction of mode in quantum well

$$\Gamma_w = \Gamma \frac{L_z}{d_{op}}$$

optical confinement factor
 quantum well thickness
 effective width of optical mode

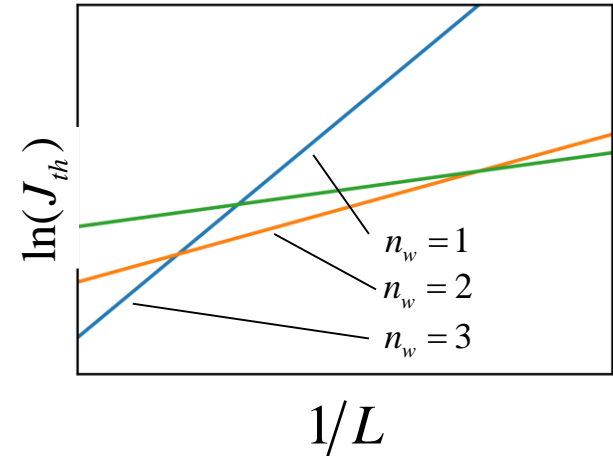
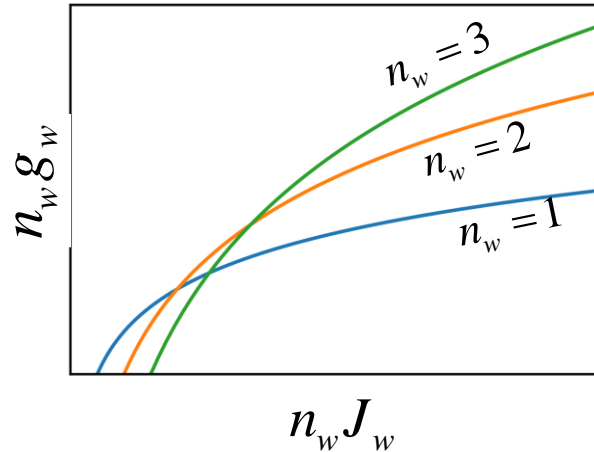


Threshold current and gain in active region with multiple quantum wells

$$n_w g_w = n_w g_0 \ln \left(\frac{n_w J_w}{n_w J_0} \right)$$

Note: $J_{th} = \frac{n_w J_w}{\eta_i}$

threshold current
at device terminals



Then: $J_{th} = \frac{n_w J_0}{\eta_i} \exp \left(\frac{g_w}{g_0} \right)$

$$J_{th} = \frac{n_w J_0}{\eta_i} \exp \left(\frac{1}{n_w \Gamma_w g_0} \left[\alpha_i + \frac{1}{2L} \ln \frac{1}{R_1 R_2} \right] \right)$$

$$I_{th} = \frac{w L n_w J_0}{\eta_i} \exp \left(\frac{1}{n_w \Gamma_w g_0} \left[\alpha_i + \frac{1}{2L} \ln \frac{1}{R_1 R_2} \right] \right)$$

w : active region width

L : active region length

Active region optimization

Optimize cavity length (L) or a fixed number of quantum wells

$$\frac{\partial I_{th}}{\partial L} = 0 \rightarrow L_{opt} = \frac{1}{2} \frac{1}{n_w \Gamma_w g_0} \ln \left(\frac{1}{R_1 R_2} \right)$$

Optimize number of quantum wells (n_w) for a fixed cavity length

$$\frac{\partial I_{th}}{\partial n_w} = 0 \rightarrow n_{opt} = \frac{1}{\Gamma_w g_0} \left(\alpha_i + \frac{1}{2L} \ln \frac{1}{R_1 R_2} \right)$$

For a general cavity, $\frac{1}{\tau_p \nu_g} = \left(\alpha_i + \frac{1}{2L} \ln \frac{1}{R_1 R_2} \right)$

$$Q = \omega_0 \tau_p$$

therefore, $n_{opt} = \frac{1}{\Gamma_w g_0 \nu_g} \frac{\omega_0}{Q}$

Additional details on the “ABC” approximation

Recombination rate in LED or Laser at or below threshold:

$$\begin{aligned} R &= R_{SRH} + R_{sp} + R_{Auger} \\ &\simeq An + Bn^2 + Cn^3 \quad \text{“ABC” approximation} \end{aligned}$$

The ABC approximation is widely used to estimate recombination rates in LEDs and lasers (at or below threshold). Although strictly speaking, it is valid only when Boltzmann statistics are valid so some care needs to be applied when using the approximation.

We have already proved that the spontaneous emission rate has an n^2 dependence (when Boltzmann statistics apply). See the previous lecture on spontaneous emission.

Let’s look at the Shockley-Reed-Hall and Auger rates.

Shockley-Reed-Hall recombination

The derivation of the SRH rate is found in many basic semiconductor textbooks.

$$R_{SRH} \approx \frac{n_0 \delta n + p_0 \delta n + \delta n^2}{C_p^{-1} (n_0 + n_{ds} + \delta n) + C_n^{-1} (p_0 + p_{ds} + \delta n)}$$

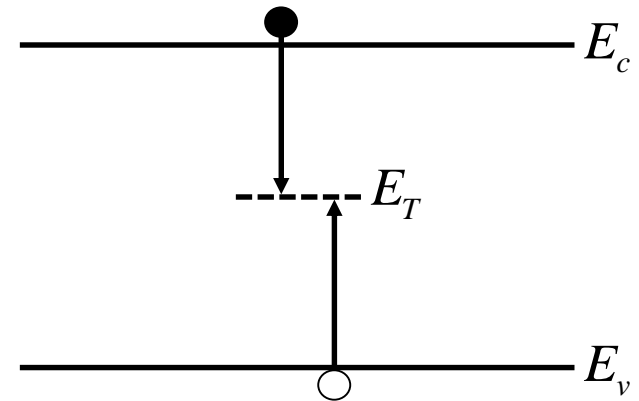
$$\begin{aligned} n &= n_0 + \delta n & n_{ds} \text{ and } p_{ds} \text{ are the electron and} \\ p &= p_0 + \delta p & \text{hole concentrations when the Fermi} \\ \delta_n &= \delta_p & \text{level is at the defect state energy} \end{aligned}$$

$$\left. \begin{aligned} C_n &= \sigma_n v_{n,th} N_{ds} \\ C_p &= \sigma_p v_{p,th} N_{ds} \end{aligned} \right\} \text{Capture rates}$$

$$\left. \begin{aligned} \sigma_n \\ \sigma_p \end{aligned} \right\} \text{Capture cross-sections}$$

$$\left. \begin{aligned} v_n \\ v_p \end{aligned} \right\} \text{Thermal velocity}$$

$$N_{ds} : \text{defect density}$$



We see that in general we cannot write

$$R_{SRH} = An$$

But, we can do so if we restrict our analysis to a “low-injection” or “high-injection” regime.

Low-injection and high-injection regime

Active region materials have a background doping due to unintentional doping impurities introduced during growth. Let's assume our active region is unintentionally doped p-type.

$p_0 \gg \delta_n$ Low-injection regime

$$R_{SRH} = \frac{n_0 \delta n + p_0 \delta n + \delta n^2}{C_p^{-1}(n_0 + n_{ds} + \delta n) + C_n^{-1}(p_0 + p_{ds} + \delta n)} \cong C_n \delta_n \approx A_{low} n$$

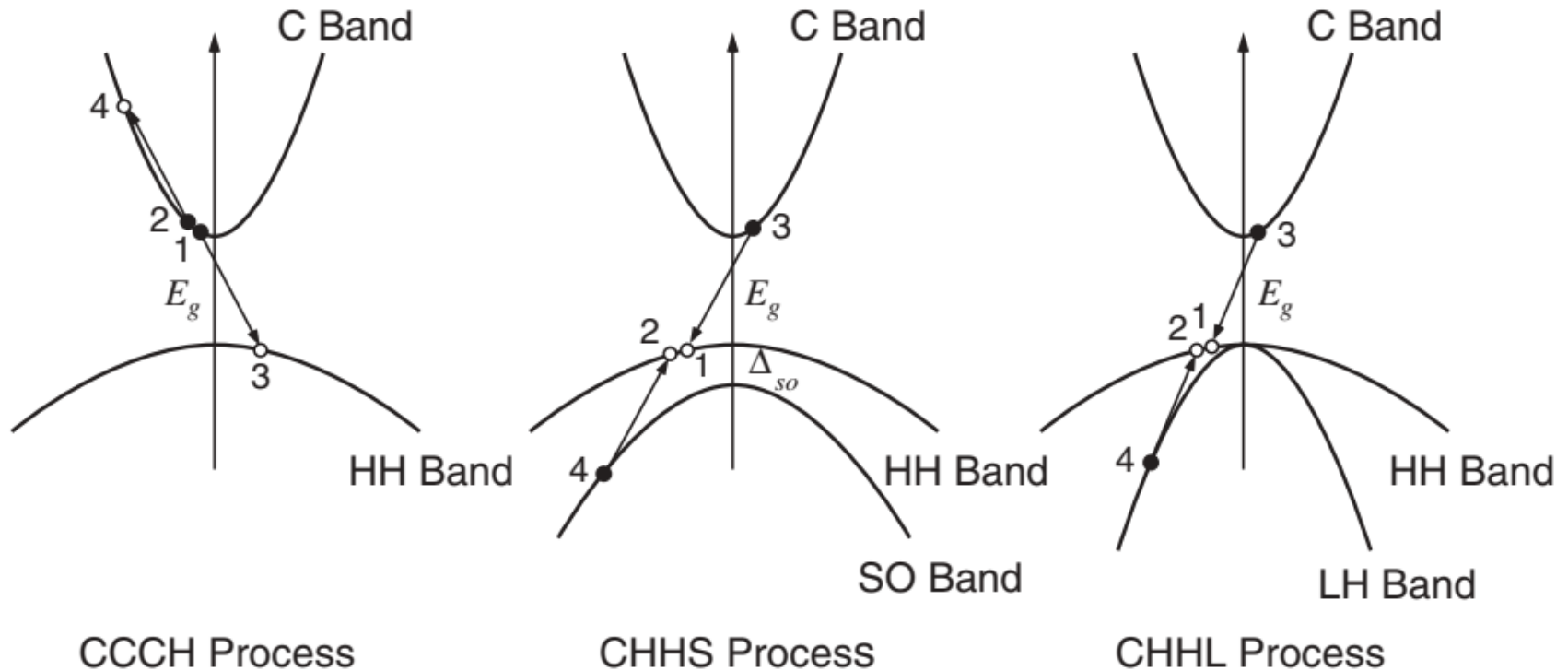
$\delta_n \gg p_0$ High-injection regime

$$R_{SRH} \cong \frac{C_n C_p}{C_n + C_p} \delta_n \approx A_{high} n$$

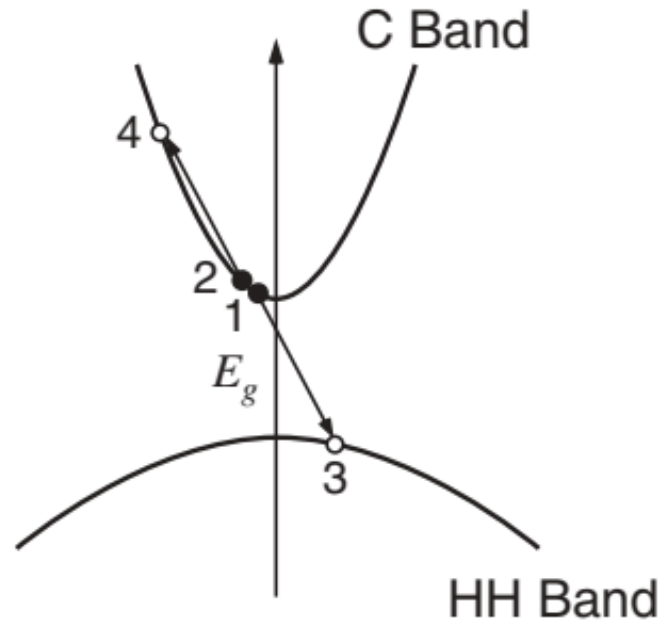
We see that we can write $R_{SRH} = An$ so long we stay in one of the two regimes. If the electron capture is the rate-limiting step (for p-type material), then the A coefficient will be identical in both regimes.

Auger recombination

Electron recombines with hole and gives up excess energy to another carrier instead of releasing a photon. Several different Auger processes are possible (as shown below). Often there is a material-dependent dominant process.



Auger recombination



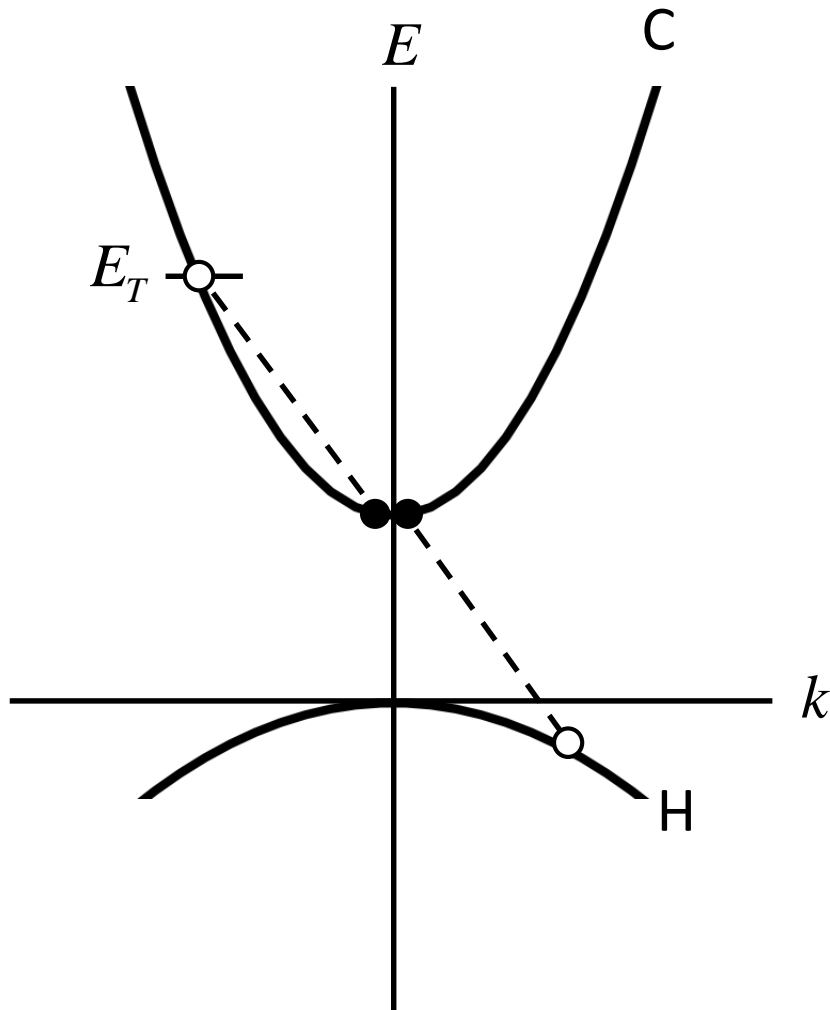
The CCCH Auger rate is given by

$$\begin{aligned}
 R_{Auger} &= C_0 f_1 f_2 (1 - f_3) (1 - f_4) \\
 &= C_0 \exp\left[\frac{F_c - E_1}{kT}\right] \exp\left[\frac{F_c - E_2}{kT}\right] \exp\left[\frac{E_3 - F_v}{kT}\right] \quad (1) \\
 &= C_0 \frac{n^2 p}{(kT)^2 N_c^2 N_v} \exp\left[\frac{E_g - E_4}{kT}\right]
 \end{aligned}$$

Very likely that State 4 is empty since it is well beyond the band edge

$$R_{Auger} = C n^2 p = C n^3 \quad \text{for } n = p$$

Auger recombination



Energy and momentum conservation needs to be simultaneously conserved. This sets a threshold value for E_4 which we call E_T . Materials with small E_T will have large Auger rates since

$$R_{Auger} \propto \exp(-E_T / kT)$$

E_T is related to the curvature of the bands through

$$E_T = \frac{2m_e^* + m_h^*}{m_e^* + m_h^*} E_g = aE_g$$

the value of a is approximately unity for III-V semiconductors therefore,

$$R_{Auger} \propto \exp(-E_g / kT)$$

Auger recombination is higher in low bandgap materials.